

# STA 215 Definitions and Interpretations Guide

## Grand Valley State University

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**Note:** The following guide provides definitions of commonly found symbols and topics in statistics and formatting of common statistical interpretations.

### Statistical Symbols:

$\mu$ : Population mean	$\hat{y}$ : Predicted $y$ value in linear regression
$\bar{x}$ : Sample mean	$H_0$ : Null hypothesis
$p$ : Population proportion	$H_a$ : Alternative hypothesis
$\hat{p}$ : Sample proportion	$\alpha$ : Significance level
$\sigma$ : Population standard deviation	$z$ : Z-score
$s$ : Sample standard deviation	$t$ : t-test statistic
$\sigma^2$ : Population variance	$\mu_1, \mu_2$ : Population mean of population 1 and 2 respectively
$s^2$ : Sample variance	$\bar{x}_1, \bar{x}_2$ : Sample mean of sample 1 and 2 respectively
$n$ : Sample size	$\mu_d$ : Difference in population means (usually $\mu_1 - \mu_2$ )
$z^*, t^*$ : Critical values (confidence interval multipliers)	$\bar{x}_d$ : Difference in sample means (usually $\bar{x}_1 - \bar{x}_2$ )
$r$ : Pearson's correlation coefficient for a sample	$p_1, p_2$ : Population proportion of population 1 and 2
$R^2$ : Coefficient of determination	$\hat{p}_1, \hat{p}_2$ : Sample proportion of sample 1 and 2
$\hat{\beta}_0$ : Estimated $y$ -intercept for linear regression	$\Sigma$ : Summation
$\hat{\beta}_1$ : Estimated slope for linear regression	$\chi^2$ : Chi-square test statistic

### Interpretations in Statistics:

For the following interpretations, fill in each part of the sentence(s) that are in bold and underlined, such as: **parameter**.

Be sure to write the parameter for confidence intervals out in words to provide further context in your interpretation. For confidence intervals for differences in two parameters, be sure to state which one is greater/lesser and why.

#### Confidence Intervals:

We are **Confidence Level**% confident that the true **parameter** is between **Lower limit** and **Upper limit**.

#### P-values:

Assuming  $H_0$  is true, the probability of obtaining the value of our observed test statistic or one more extreme is **p-value**.

For concluding hypothesis testing, make sure to write out the  $H_0$  and  $H_a$  in words. This provides further context in your conclusion.

#### Rejecting $H_0$ :

Since our p-value is **less than/equal to  $\alpha$** , we have sufficient evidence to reject  **$H_0$**  and will support  **$H_a$** .

#### Failing to reject $H_0$ :

Since our p-value is greater than  **$\alpha$** , we fail to reject  **$H_0$**  and lack sufficient evidence to support  **$H_a$** .

#### Coefficient of Determination ( $R^2$ ):

**$R^2 \cdot 100$** % of the variation in **response variable** is accounted for by **explanatory variable**.

#### Slope in linear regression:

For every 1 **unit** increase in **explanatory variable**, we expect **response variable** to **increase/decrease** by  **$|\hat{\beta}_1|$** .

#### Y- Intercept:

The predicted value of **response variable** when **explanatory variable** is 0, is  **$\hat{\beta}_0$** .

#### Residuals:

Having a negative residual means that the predicted value from our linear regression equation is too high. Moreover, if we have a positive residual it means that the predicted value was too low.